



# Modeling Spatial Patterns in Weather and Crop Yields



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## Introduction

- The rapidly growing availability and accessibility of spatially-explicit weather and climate data
- Relatively less attention to spatial correlation in weather variables and econometric methods
- Two approaches in the previous literature
  - Applied economics: Conley's Method
  - Spatial econometrics
- Reasoning for specification strategy in modeling spatial patterns is not stated explicitly
- Research Question: Which specification strategy of spatial correlation performs best in terms of prediction capability?

## An Example Model: Crop Yield Response

- Schlenker and Roberts (2009)

$$y_{it} = \int_{\bar{h}} g(h) \phi_{it} dh + \gamma_1 P_{it} + \gamma_2 P_{it}^2 + \gamma_3 t + \gamma_4 t^2 + \mu_i + \varepsilon_{it}$$

- Very popular non-Ricardian model in climate-yield literature
- Spatial correlation in the VC matrix
  - To take into account omitted weather variable bias
- This study argues that the main reason for spatial correlation in the VC matrix is aggregation bias rather than omitted weather variables
- Six comparable models are specified and prediction performance is compared

## Model Specifications

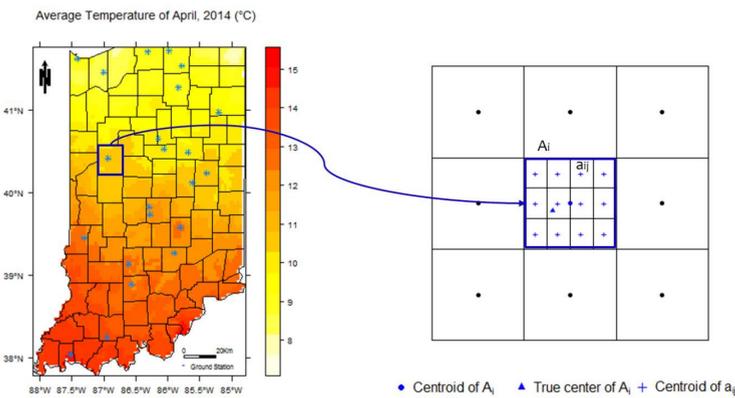
### Specification Motivations and Models

Motivation	Fixed Effects Model	Random Effects Model with Soil Vars.
Aggregation Bias	FE (Schlenker and Roberts, 2009)	
Omitted Socio-economic Vars.	FE SLAG ( $\rho W \gamma$ )	
Omitted Weather Vars.		RE, KKP-RE (Auffhammer et al., 2013)
Geophysical Process	SLX ( $WC\theta$ )	

## Models Compared

- Pooled Regression
 
$$y_{it} = \int_{\bar{h}} g(h) \phi_{it} dh + \gamma_1 P_{it} + \gamma_2 P_{it}^2 + \gamma_3 t + \gamma_4 t^2 + \varepsilon_{it}$$
- FE (Schlenker and Roberts, 2009): aggregation bias
 
$$y_{it} = \int_{\bar{h}} g(h) \phi_{it} dh + \gamma_1 P_{it} + \gamma_2 P_{it}^2 + \gamma_3 t + \gamma_4 t^2 + \mu_i + \varepsilon_{it}$$
- FE Spatial Lag (FE-SLAG): Omitted socio-economic vars.
 
$$y_{it} = \rho W_i y_t + \int_{\bar{h}} g(h) \phi_{it} dh + \gamma_1 P_{it} + \gamma_2 P_{it}^2 + \gamma_3 t + \gamma_4 t^2 + \mu_i + \varepsilon_{it}$$
- Spatial Lagged X (SLX): geophysical process of weather Vars.
 
$$y_{it} = \int_{\bar{h}} g(h) \phi_{it} dh + \gamma_1 P_{it} + \gamma_2 P_{it}^2 + \gamma_3 t + \gamma_4 t^2 + W_{it} C_{jt} \theta + \mu_i + \varepsilon_{it}$$
- RE: Omitted Weather Vars.
 
$$y_{it} = \int_{\bar{h}} g(h) \phi_{it} dh + \gamma_1 P_{it} + \gamma_2 P_{it}^2 + \gamma_3 t + \gamma_4 t^2 + \gamma S_i + \varepsilon_{it}$$
- Kapoor, Kelejian, and Prucha RE (KKP-RE): RE + KKP error structure  $u_N = \rho(I_T \otimes W_N)u_N + \varepsilon_N$

## Aggregation Bias



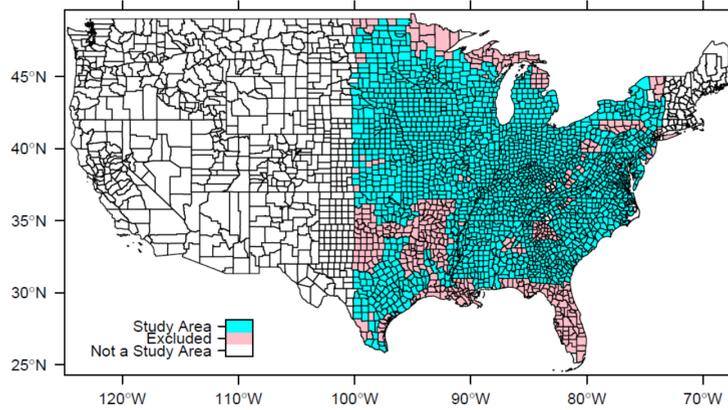
Temperature at j-th cell of i-th county ( $H_{ij}$ )

$$H_{ij} = \underbrace{\bar{H}_i}_{\text{county average}} + \underbrace{\nu_{ij}}_{\text{cell-level variation}} = \sum_{j=1}^{n_i} w_{ij} H_{ij} + \nu_{ij}$$

- The error terms absorb all spatial variation

- Proposition 1**  
The larger the aggregation losses, the less spatial variation.  
 $\lim_{n_i \rightarrow \infty} \sum_{j=1}^{n_i} |\nu_{ij}|$  does not define.
- Proposition 2**  
The larger aggregation has the less spatial correlation.  
 $\rho_k \leq \rho_l$  when  $k$  is larger aggregation level than  $l$
- Proposition 3**  
The areal center of weather variable is unknown.  
Distance based (fixed) weights matrix could be inappropriate.  
⇒ Conley's or SHAC estimator

## Data

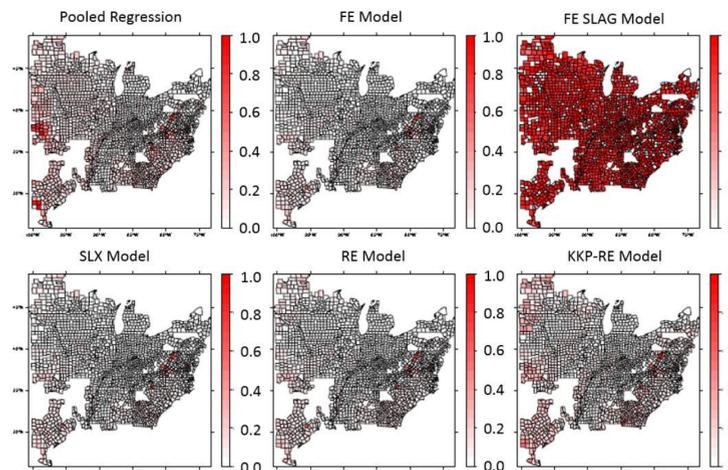


Study Areas: (1,964 counties X 33 years) Balanced Panel

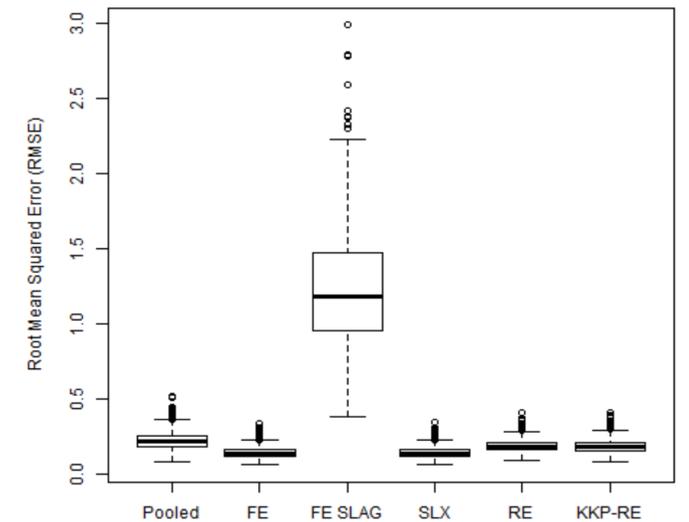
- Non-agricultural land masked out  
1992 LandSat (USGS, 30m X 30 m) applied
- Corn yields  
NASS county-level yields from 1981 – 2013
- Counties are based on 2013 (500K map) from the Census Bureau
- Temperature and total precipitation  
PRISM (Oregon State University, 4 Km X 4 Km)
- Soil Variables  
gSSURGO (NRCS, 10m X 10m)

## Results

### In Sample Prediction



Out of Sample Prediction (1,000 Simulations):  
27 years for estimation / 6 years for prediction



- Best performance: SLX ~ FE and KKP-RE ~ RE
- FE-SLAG performed worst in our sample

## Conclusion

- Aggregation bias is one of the major sources of spatial correlation in addition to omitted variables and geophysical processes
- Depending upon the causes of spatial correlation, specification of the regression equation can be different
- Soil characteristic should be included in RE specification
- SHAC estimator provide tighter CI band estimates
- ❖ Consider economic and geophysical reasoning more to guide model selection in prediction capability of crop yield response function

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